

---

---

**Road vehicles — Lateral transient  
response test methods — Open-loop test  
methods**

*Véhicules routiers — Méthodes d'essai de réponse transitoire  
latérale — Méthodes d'essai en boucle ouverte*





**COPYRIGHT PROTECTED DOCUMENT**

© ISO 2011

All rights reserved. Unless otherwise specified, no part of this publication may be reproduced or utilized in any form or by any means, electronic or mechanical, including photocopying and microfilm, without permission in writing from either ISO at the address below or ISO's member body in the country of the requester.

ISO copyright office  
Case postale 56 • CH-1211 Geneva 20  
Tel. + 41 22 749 01 11  
Fax + 41 22 749 09 47  
E-mail [copyright@iso.org](mailto:copyright@iso.org)  
Web [www.iso.org](http://www.iso.org)

Published in Switzerland

Licensed by SOURCE to ISO/TC 22/SC 9  
Downloaded: 2011-04-22  
Single-user licence only, copying and networking prohibited.

# Contents

Page

|  |           |
|--|-----------|
| Foreword .....   | iv        |
| Introduction.....  | v         |
| <b>1 Scope .....</b>   | <b>1</b>  |
| <b>2 Normative references .....</b>                                    | <b>1</b>  |
| <b>3 Terms and definitions .....</b>                                   | <b>1</b>  |
| <b>4 General conditions .....</b>                                      | <b>1</b>  |
| <b>5 Principle .....</b>   | <b>2</b>  |
| <b>6 Reference system.....</b>   | <b>3</b>  |
| <b>7 Variables.....</b>  | <b>3</b>  |
| <b>8 Measuring equipment .....</b>                                     | <b>4</b>  |
| <b>9 Test conditions .....</b>   | <b>4</b>  |
| <b>10 Step input .....</b>   | <b>5</b>  |
| <b>11 Sinusoidal input — one period (see ISO/TR 8725).....</b>         | <b>7</b>  |
| <b>12 Random input (see ISO/TR 8726).....</b>                          | <b>9</b>  |
| <b>13 Pulse input .....</b>  | <b>11</b> |
| <b>14 Continuous sinusoidal input.....</b>                             | <b>12</b> |
| <b>Annex A (normative) Test report — General data .....</b>            | <b>14</b> |
| <b>Annex B (normative) Test report — Presentation of results .....</b> | <b>16</b> |
| <b>Bibliography.....</b>   | <b>22</b> |

## Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 7401 was prepared by Technical Committee ISO/TC 22, *Road vehicles*, Subcommittee SC 9, *Vehicle dynamics and road-holding ability*.

This third edition cancels and replaces the second edition (ISO 7401:2003), which has been technically revised.

## Introduction

The main purpose of this International Standard is to provide repeatable and discriminatory test results.

The dynamic behaviour of a road vehicle is a very important aspect of active vehicle safety. Any given vehicle, together with its driver and the prevailing environment, constitutes a closed-loop system that is unique. The task of evaluating the dynamic behaviour is therefore very difficult since the significant interaction of these driver-vehicle-environment elements is each complex in itself. A complete and accurate description of the behaviour of the road vehicle must necessarily involve information obtained from a number of different tests.

Since this test method quantifies only one small part of the complete vehicle handling characteristics, the results of these tests can only be considered significant for a correspondingly small part of the overall dynamic behaviour.

Moreover, insufficient knowledge is available concerning the relationship between overall vehicle dynamic properties and accident avoidance. A substantial amount of work is necessary to acquire sufficient and reliable data on the correlation between accident avoidance and vehicle dynamic properties in general and the results of these tests in particular. Consequently, any application of this test method for regulation purposes will require proven correlation between test results and accident statistics.



# Road vehicles — Lateral transient response test methods — Open-loop test methods

## 1 Scope

This International Standard specifies open-loop test methods for determining the transient response behaviour of road vehicles. It is applicable to passenger cars, as defined in ISO 3833, and to light trucks.

NOTE The open-loop manoeuvres specified in this International Standard are not representative of normal driving conditions, but are nevertheless useful for obtaining measures of vehicle transient behaviour in response to several specific types of steering input under closely controlled test conditions. For measurements of steady-state properties, see ISO 4138.

## 2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 1176:1990, *Road vehicles — Masses — Vocabulary and codes*

ISO 2416:1992, *Passenger cars — Mass distribution*

ISO/TR 8725:1988, *Road vehicles — Transient open-loop response test method with one period of sinusoidal input*

ISO/TR 8726:1988, *Road vehicles — Transient open-loop response test method with pseudo-random steering input*

ISO 8855<sup>1)</sup>, *Road vehicles — Vehicle dynamics and road-holding ability — Vocabulary*

ISO 15037-1:2006, *Road vehicles — Vehicle dynamics test methods — Part 1: General conditions for passenger cars*

## 3 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO 8855 apply.

## 4 General conditions

The general conditions specified in ISO 15037-1 shall apply.

---

1) To be published.

## 5 Principle

### 5.1 General

**IMPORTANT** — The method of data analysis in the frequency domain assumes that the vehicle has a linear response; this is unlikely to be the case over the whole range of lateral accelerations of interest. The standard method of dealing with such a situation is to restrict the input to a sufficiently small range such that linear behaviour can be assumed. If necessary, testing can be performed with several ranges of inputs that, together, cover the entire range of interest.

The primary object of these tests is to determine the transient response behaviour of a vehicle. Characteristic values and functions in the time and frequency domains are considered necessary for characterizing vehicle transient response.

Important characteristics in the time domain are:

- a) time lags between steering-wheel angle, lateral acceleration and yaw velocity;
- b) response times of lateral acceleration and yaw velocity (see 10.2.1 and 10.2.2);
- c) lateral acceleration gain (lateral acceleration divided by steering-wheel angle);
- d) yaw velocity gain (yaw velocity divided by steering-wheel angle); and
- e) overshoot values (see 10.2.3).

These characteristics show correlation with subjective evaluation during road driving.

Important characteristics in the frequency domain are the frequency responses, i.e. amplitudes and phases of:

- lateral acceleration related to steering-wheel angle; and
- yaw velocity related to steering-wheel angle.

### 5.2 Test methods

There are several test methods for obtaining these characteristics in the domains of time and frequency, the applicability of which depends in part on the size of the test track available.

- a) Time domain:
  - 1) step input; and
  - 2) sinusoidal input (one period).
- b) Frequency domain:
  - 1) random input;
  - 2) pulse input; and
  - 3) continuous sinusoidal input.

These test methods are optional, but at least one of each domain type should be performed. The methods chosen shall be indicated in the general data specified in Annex A and in the presentation of test results specified in Annex B.



It is possible that the characteristic values of lateral acceleration gain and yaw velocity gain, obtained by the different test methods, may not be comparable, owing to one or more of the following circumstances:

- linear versus non-linear vehicle behaviour;
- periodic versus non-periodic steady-state condition;
- steady state versus dynamic vehicle behaviour.

## 6 Reference system

The reference system specified in ISO 15037-1 shall apply.

The location of the origin of the vehicle axis system ( $X_V$ ,  $Y_V$ ,  $Z_V$ ) is the reference point and therefore should be independent of the loading condition. It is fixed in the longitudinal plane of symmetry at half-wheelbase and at the same height above the ground as the centre of gravity of the vehicle at complete vehicle kerb mass (see ISO 1176).

## 7 Variables

The following variables shall be determined:

- a) steering-wheel angle,  $\delta_H$ ;
- b) lateral acceleration,  $a_Y$ ;
- c) yaw velocity,  $\dot{\psi}$ ;
- d) longitudinal velocity,  $v_X$ .

The following variables may be determined:

- roll angle,  $\phi$ ;
- sideslip angle,  $\beta$ ;
- lateral velocity,  $v_Y$ ;
- steering-wheel torque,  $M_H$ .

These variables, defined in ISO 8855, are not intended to comprise a complete list.

## 8 Measuring equipment

### 8.1 Description

Subclause 4.1 of ISO 15037-1:2006 shall apply as well as the following additions shown in Table 1.

**Table 1 — Variables, typical operating ranges and recommended maximum errors**

| Variable             | Range                       | Recommended maximum error of the combined transducer/ recorder system |
|----------------------|-----------------------------|---|
| Steering-wheel angle | -180° to +180° <sup>a</sup> | ±1°   |
| Yaw velocity         | -50 °/s to +50 °/s          | ±0,5 °/s  |
| Lateral velocity     | -10 m/s to +10 m/s          | ±0,1 m/s  |
| Sideslip angle       | -15° to +15°                | ±0,3°   |

<sup>a</sup> Assuming a conventional steering system.

The use of a programmable steer robot may help to increase the accuracy and repeatability of steer inputs for the described transient response manoeuvres.

### 8.2 Transducer installation

Subclause 4.2 of ISO 15037-1:2006 shall apply.

### 8.3 Data processing

The recording system and data processing requirements contained in 4.3 of ISO 15037-1:2006 shall apply.

## 9 Test conditions

### 9.1 General

The test conditions specified in Clause 5 of ISO 15037-1:2006 shall apply.

### 9.2 Vehicle loading conditions

#### 9.2.1 General

Tests shall be carried out at the minimum loading condition and at the maximum loading condition defined below, and at other loading conditions of interest.

In accordance with ISO 1176:1990, 4.8 and 4.13, the maximum authorized total mass (Code: ISO-M08) and the maximum authorized axle load (Code: ISO-M13) shall not be exceeded.

Care shall be taken to minimize the difference of both the location of the centre of gravity and the moments of inertia as compared to the loading conditions of the vehicle in normal use (see ISO 2416:1992, Clause 4). The resulting static wheel loads shall be determined and recorded in the test report (see Annex A).

### 9.2.2 Minimum loading condition

For the minimum loading condition, the total vehicle mass shall consist of the complete vehicle kerb mass (Code: ISO-M06) in accordance with ISO 1176:1990, 4.6, plus the masses of the driver and the instrumentation. The mass of the driver and the instrumentation should not exceed 150 kg. The load distribution shall be equivalent to that of two occupants in the front seats, in accordance with ISO 2416.

### 9.2.3 Maximum loading condition

For the maximum loading condition, the total mass shall be equal to the maximum authorized total mass.

For the maximum loading condition, the total mass shall be equivalent to the complete vehicle kerb mass, plus 68 kg for each seat in the passenger compartment and with the remaining maximum mass of transportable goods equally distributed over the luggage compartment in accordance with ISO 2416. Loading of the passenger compartment shall be such that the actual wheel loads are equal to those obtained by loading each seat with 68 kg according to ISO 2416.

The transient lateral response is strongly influenced by the moments of inertia and by the height of the centre of gravity. Wheel loads define only one of several factors contributing to the dynamic properties of vehicles. Care shall be taken to keep test conditions between test runs as constant as possible. Therefore, it is recommended to limit weight changes caused by fuel consumption.

## 9.3 Warm-up

The warm-up procedures specified in 6.1 of ISO 15037-1:2006 shall apply.

## 9.4 Test speed

The test speed is defined as the nominal value of the longitudinal velocity. The standard test speed is 100 km/h. Other test speeds of interest may be used (preferably in 20 km/h steps).

# 10 Step input

## 10.1 Test procedure

Drive the vehicle at the test speed (see 9.4) in a straight line. The initial speed shall not deviate by more than 2 km/h from the test speed. Starting from a  $0\text{ }^\circ/\text{s} \pm 0,5\text{ }^\circ/\text{s}$  yaw velocity equilibrium condition, apply a steering input as rapidly as possible to a preselected value and maintain at that value for several seconds after the measured vehicle motion variables have reached a steady state. In order to keep the steering input short relative to the vehicle response time, the time between 10 % and 90 % of the steering input should not be greater than 0,15 s. No change in throttle position shall be made, although speed may decrease. A steering-wheel stop may be used for selecting the input angle.

Take data for both left and right turns. All data shall be taken in one direction followed by all data in the other direction. Alternatively, take data successively in each direction for each acceleration level, from the lowest to the highest level, this being preferable with respect to tyre wear and symmetrical vehicle stress. Record the method chosen in the test report (see Annex A).

Data shall be taken throughout the desired range of steering inputs and response variable outputs.

Determine the steering-wheel angle amplitude by steady-state driving on a circle the radius of which gives the preselected steady-state lateral acceleration at the required test speed. The standard steady-state lateral acceleration level is  $4\text{ m/s}^2$ . Additional levels of  $2\text{ m/s}^2$  and  $6\text{ m/s}^2$  may be used.

Perform all test runs at least three times.

## 10.2 Data analysis

### 10.2.1 Response time

The transient-response data reduction shall be carried out such that the origin for each response is the time at which the steering-wheel angle change is 50 % complete. This is the reference point from which all response times are measured. Response time is thus defined as the time, measured from this reference, for the vehicle transient response to first reach 90 % of its new steady-state value (see Figure 1).

### 10.2.2 Peak response time

The peak response time is the time, measured from the reference point, for a vehicle transient response to reach its peak value (see Figure 1).

In some instances, system damping can be so high that a peak value cannot be determined. If this occurs, data sheets should be marked accordingly.

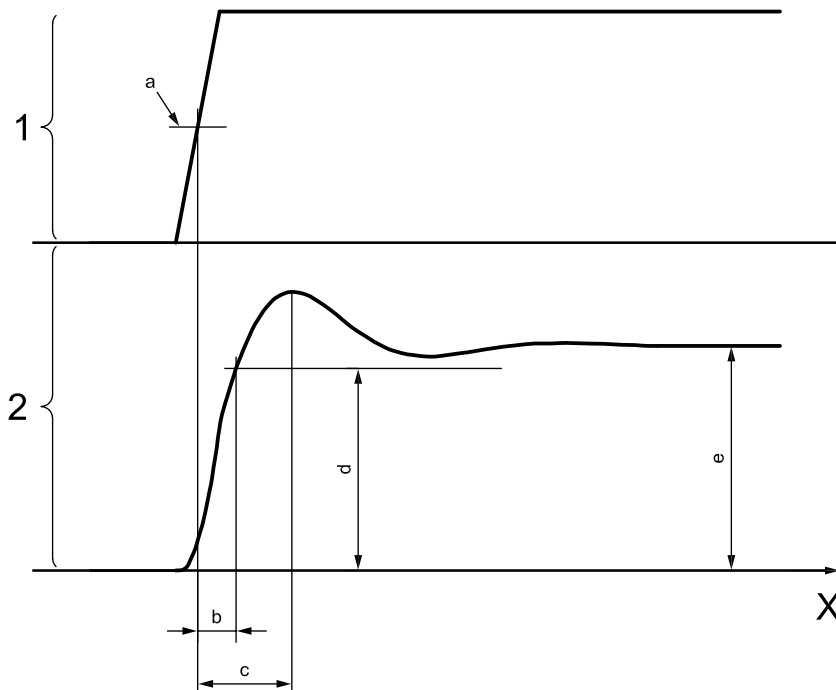
### 10.2.3 Overshoot values

The overshoot values are calculated as a ratio: the difference of peak value and steady-state value divided by steady-state value.

## 10.3 Data presentation

### 10.3.1 General

General data shall be presented in accordance with Annex A.



#### Key

- |                         |                             |                      |
|-------------------------|-----------------------------|----------------------|
| 1 steering-wheel input  | a 50 % level.               | d 90 % steady state. |
| 2 vehicle response time | b Response time; T.         | e Steady state.      |
| X time                  | c Peak response time; Tmax. |                      |

**Figure 1 — Response time and peak response time**

Licensed by SOURCE to ISO/TC 22/SC 9  
 Downloaded: 2011-04-22  
 Single-user licence only, copying and networking prohibited.

### 10.3.2 Time histories

The time histories of variables used for data evaluation shall be plotted. If a curve is fitted to any set of data, the method of curve fitting shall be described in the presentation of results in Annex B.

Plot the time histories of steering-wheel angle, lateral acceleration and yaw velocity for each measured lateral acceleration level in the form, as shown in Figure B.1.

### 10.3.3 Time response data summary

Record the following values in accordance with Table B.1 for each combination of test speed and lateral acceleration:

- a) steady-state yaw velocity response gain,  $\left(\frac{\dot{\psi}}{\delta_H}\right)_{ss}$  ;
- b) lateral acceleration response time,  $T_{aY}$ ;
- c) yaw velocity response time,  $T_{\dot{\psi}}$ ;
- d) lateral acceleration peak response time,  $T_{aY,max}$ ;
- e) yaw velocity peak response time,  $T_{\dot{\psi},max}$ ;
- f) overshoot value of lateral acceleration,  $U_{aY}$ ;
- g) overshoot value of yaw velocity,  $U_{\dot{\psi}}$ .

## 11 Sinusoidal input — one period (see ISO/TR 8725)

### 11.1 Test procedure

Drive the vehicle at the test speed (see 9.4) in a straight line. The initial speed shall not deviate by more than 2 km/h from the test speed. Starting from a  $0\text{ }^\circ/\text{s} \pm 0,5\text{ }^\circ/\text{s}$  yaw velocity equilibrium condition, apply one full period sinusoidal steering-wheel input with a frequency of 0,5 Hz. An additional frequency of 1 Hz should also be used. The amplitude error of the actual waveform compared to the true sine wave shall be less than 5 % of the first peak value. No change in throttle position shall be made, although speed may decrease.

Take data while the steering-wheel is rotated, initially both to the left and to the right. All data shall be taken in one direction followed by all data in the other direction. Alternatively, take data successively in each direction for each acceleration level, from the lowest to the highest level. Record the method chosen in the test report (see Annex A).

Increase the steering-wheel input stepwise up to a magnitude sufficient to produce the desired lateral acceleration in accordance with 11.2.2. The standard lateral acceleration level is  $4\text{ m/s}^2$ . Additional acceleration levels of  $2\text{ m/s}^2$  and  $6\text{ m/s}^2$  and up to the adhesion limit (see ISO/TR 8725) may be used.

Perform at least three test runs for each combination of speed and steering.

## 11.2 Data analysis

### 11.2.1 General

The test results can be sensitive to the method of data processing. The procedure given in ISO/TR 8725 should therefore be used.

### 11.2.2 Lateral acceleration

Lateral acceleration in this test is defined as the first peak value of the lateral acceleration time history, corrected for vehicle roll angle.

### 11.2.3 Yaw velocity

Yaw velocity in this test is defined as the first peak value of the yaw velocity time history.

### 11.2.4 Time lags

The time lags between the variables steering-wheel angle, lateral acceleration and yaw velocity are calculated for the first and second peaks by means of cross-correlation of the first and second half-waves, respectively (positive and negative parts of the time history).

### 11.2.5 Lateral acceleration gain

Lateral acceleration gain is calculated as the ratio of the lateral acceleration (in accordance with 11.2.2) to the corresponding peak value of the steering-wheel angle.

### 11.2.6 Yaw velocity gain

Yaw velocity gain is calculated as the ratio of the yaw velocity (according to 11.2.3) to the corresponding peak value of the steering-wheel angle.

## 11.3 Data presentation

### 11.3.1 General

General data shall be presented in accordance with Annex A.

The time histories of variables used for data evaluation shall be plotted. If a curve is fitted to any set of data, the method of curve fitting shall be described in the presentation of results in accordance with Annex B.

### 11.3.2 Time histories

Plot the time histories of steering-wheel angle, lateral acceleration and yaw velocity for each measured lateral acceleration level as shown in Figure B.2.

### 11.3.3 Time response data summary

Calculate the following test data (see Table B.2) as mean values  $\pm$  standard deviation:

a) time lags between steering-wheel angle and lateral acceleration

1) first peak,  $T(\delta_H - a_Y)_1$

2) second peak,  $T(\delta_H - a_Y)_2$

b) time lags between steering-wheel angle and yaw velocity

1) first peak,  $T(\delta_H - \dot{\psi})_1$

2) second peak,  $T(\delta_H - \dot{\psi})_2$

c) lateral acceleration gain,  $\frac{a_Y}{\delta_H}$

d) yaw velocity gain,  $\frac{\dot{\psi}}{\delta_H}$

#### 11.3.4 Data as functions of lateral acceleration

If optional lateral acceleration levels are measured, it is useful to present data as functions of lateral acceleration.

#### 11.3.5 Asymmetry factors

The justification for making two initial turn directions is that an asymmetry can exist. This asymmetry can be presented in terms of asymmetry factors (see ISO/TR 8725).

## 12 Random input (see ISO/TR 8726)

### 12.1 Test procedure

Make the test runs by driving the vehicle at the required test speed (see 9.4) while making continuous inputs to the steering-wheel, up to predetermined limits of steering-wheel angle.

The test shall cover a minimum frequency range of 0,2 Hz to 2 Hz. Optionally, the frequency range may also be extended above and below these limits.

Do not use mechanical limiters of the steering-wheel angle, if existing, because of their effect on the harmonic content of the input. It is also important that the input be continuous, as periods of relative inactivity will seriously reduce the signal-to-noise ratio.

To ensure adequate high-frequency content, the input should be energetic (see 12.2.2 and 12.2.3).

To ensure enough total data, capture at least 12 min of data, unless confidence limits indicate that a shorter time is sufficient. Ideally, all data should be accomplished in a continuous run, but practical considerations can prevent this for two reasons. Firstly, the test track could be insufficiently long to permit a continuous run of such a length at the required test speed. Secondly, the computer used to analyse the data might not be large enough to handle all the data at once. In either case, data may be captured using a number of shorter runs of at least 30 s duration.

For each test run, maintain the longitudinal velocity within a tolerance of  $\pm 3$  km/h of the desired test speed.

Determine the steering-wheel angle limits by steady-state driving on a circle, the radius of which gives the preselected steady-state lateral acceleration at the required test speed. The standard steady-state lateral acceleration level is  $3 \text{ m/s}^2$  or less, as necessary to remain within the range in which the vehicle exhibits linear properties (see "IMPORTANT" in 5.1, and ISO/TR 8726). Optionally, higher lateral acceleration levels may also be used, provided the vehicle remains in the linear range.

## 12.2 Data analysis

### 12.2.1 General

The data processing can be carried out using a multi-channel real time analyser or a computer with the appropriate software (see ISO/TR 8726).

### 12.2.2 Preliminary analysis

A Fourier analysis shall be made of the steering-wheel angle time history. The result shall be displayed as a graph of the input level relative to that at the lowest frequency versus frequency, as shown in Figure B.3.

This graph shall be examined to ensure adequate frequency content. The recommended ratio between maximum and minimum steering-wheel angle should be not greater than 4:1 (12 dB). If this ratio is greater, the results may be discarded or, if used, the extent of the ratio shall be recorded in the test report (see Figure B.3).

### 12.2.3 Further data processing

The data shall then be processed using equipment appropriate for producing the transfer function amplitude and phase information together with the coherence function for the following combinations of input and output variables:

- 1) lateral acceleration related to steering-wheel angle;
- 2) yaw velocity related to steering-wheel angle.

If data has not been captured in a continuous run, calculate the auto and cross-spectral densities for each run. The results of individual runs shall then be averaged. The averaging function used shall be recorded in the test report (see Annex A).

## 12.3 Data presentation

### 12.3.1 General

General data shall be presented in accordance with Annex A.

If a curve is fitted to any set of data, the method of curve fitting shall be described in accordance with Annex B.

### 12.3.2 Frequency response functions

For each pair of input and output variables, the frequency response (i.e. gain and phase-angle functions) shall be presented on a graph as shown in Figure B.4. The figure shall be completed with the number and length of the data sequences, the averaging function, the digitizing rate and the windowing function used.

The coherence function shall also be presented on the graph (see Figure B.4). This coherence function quantifies the amount of correlated information in relation to noise present in the data. To obtain close confidence limits, it is necessary to have high coherence levels and a large number of averages.

Experience shows that coherence for yaw velocity related to steering-wheel angle shall be above 0,95 in the range from 0,2 to 2 Hz for reproducible and reliable test results.

### 12.3.3 Frequency response data summary

This is to be specified based on further test experience.



## 13 Pulse input

### 13.1 Test procedure

Drive the vehicle at the test speed (see 9.4) in a straight line. The initial speed shall not deviate by more than 2 km/h from the test speed. Starting from a  $0\text{ }^\circ/\text{s} \pm 0,5\text{ }^\circ/\text{s}$  yaw velocity equilibrium condition, apply a triangular waveform steering-wheel input, followed by 3 s to 5 s neutral steering-wheel position. No change in throttle position shall be made, although speed may decrease.

Use a pulse width of 0,3 s to 0,5 s. Make efforts to minimize the overshoot of the steering-wheel angle and the differences between zero references before and after the steering-wheel input to values  $\leq 5\%$  of the peak input level. The zero reference is the steady-state value before and after the steering-wheel input.

Determine the amplitude of the steering-wheel input by steady-state driving on a circle, the radius of which gives the preselected steady-state lateral acceleration at the required test speed. The standard steady-state lateral acceleration level is  $4\text{ m/s}^2$  or less as necessary to remain within the range in which the vehicle exhibits linear properties (see "IMPORTANT" in 5.1). Optionally, higher lateral acceleration levels may also be used, provided the vehicle remains in the linear range.

Perform all test runs at least three times.

### 13.2 Data analysis

#### 13.2.1 General

The data processing can be carried out using a multi-channel real time analyser or a computer with the appropriate software.

#### 13.2.2 Preliminary analysis

A Fourier analysis shall be made of the steering-wheel angle time history. The result shall be displayed as a graph of the input level relative to that at the lowest frequency versus frequency as shown in Figure B.3.

#### 13.2.3 Further data processing

The data shall then be processed using appropriate equipment to produce the transfer function amplitude and phase information together with the coherence function for the following combinations of input and output variables:

- 1) lateral acceleration related to steering-wheel angle;
- 2) yaw velocity related to steering-wheel angle.

The transfer functions of at least three test runs shall be averaged.

### 13.3 Data presentation

#### 13.3.1 General

General data shall be presented in accordance with Annex A.

Time histories of variables used for data evaluation shall be plotted. If a curve is fitted to any set of data, the method of curve fitting shall be described in the test report in accordance with Annex B.

### 13.3.2 Frequency response functions

For each pair of input and output variables, the frequency response (i.e. gain and phase-angle functions) shall be presented on a graph, as shown in Figure B.4. The graph shall be completed with the number and length of the data sequences, the averaging function, the digitizing rate and the windowing function used.

The coherence function shall also be presented on the graph (see Figure B.4). This function quantifies the amount of correlated information in relation to noise present in the data. To obtain close confidence limits, it is necessary to have high coherence levels and a large number of averages.

### 13.3.3 Frequency response data summary

This is to be specified based on further test experience.

## 14 Continuous sinusoidal input

### 14.1 Test procedure

Drive the vehicle at the test speed (see 9.4) in a straight line. The initial speed shall not deviate more than 2 km/h from the test speed. Starting from a  $0\text{ }^\circ/\text{s} \pm 0,5\text{ }^\circ/\text{s}$  yaw velocity equilibrium condition, apply at least three periods of sinusoidal steering-wheel input with the predetermined steering-wheel angle amplitude and frequency. No change in throttle position shall be made, although speed may decrease.

Increase the steering frequency in steps. The test shall cover a minimum frequency range of 0,2 Hz to 2 Hz. Optionally, the frequency range may also be extended above and below these limits.

Determine the steering-wheel angle amplitude by steady-state driving on a circle the radius of which gives the preselected steady-state lateral acceleration at the required test speed. The standard steady-state lateral acceleration level is  $4\text{ m/s}^2$ . Additional levels of  $2\text{ m/s}^2$  and  $6\text{ m/s}^2$  may be used.

### 14.2 Data analysis

#### 14.2.1 Amplitude

The amplitude of the steering-wheel angle, lateral acceleration and yaw velocity is defined as the mean value of the amplitudes following the first period.

All amplitudes shall be taken during the manoeuvre when the vehicle is in a periodic steady-state condition.

#### 14.2.2 Lateral acceleration gain

Lateral acceleration gain shall be calculated as the ratio of the lateral acceleration amplitude to the steering-wheel angle amplitude, both amplitudes being in accordance with 14.2.1.

#### 14.2.3 Yaw velocity gain

Yaw velocity gain shall be calculated as the ratio of the yaw velocity amplitude to the steering-wheel angle amplitude, both amplitudes being in accordance with 14.2.1.

#### 14.2.4 Phase angle

Phase angles between the steering-wheel angle and the lateral acceleration and yaw velocity shall be determined from the time histories after the first period, when the vehicle is in a periodic steady-state condition.

## **14.3 Data presentation**

### **14.3.1 General**

General data shall be presented as given on the summary form in Annex A.

Time histories of variables used for data evaluation shall be plotted. If a curve is fitted to any set of data, the method of curve fitting shall be described in the presentation of results as in Annex B.

### **14.3.2 Frequency response functions**

For each pair of the input and output variables, lateral acceleration and yaw velocity, the frequency response (i.e. gain and phase-angle functions) shall be presented on a graph as shown in Figure B.4.

### **14.3.3 Frequency response data summary**

This is to be specified based on further test experience.



**Test personnel**      Driver: .....  
Observer: .....  
Data analyst: .....

**General comments** .....  
.....  
.....  
.....  
.....  
.....

**Annex B**  
(normative)

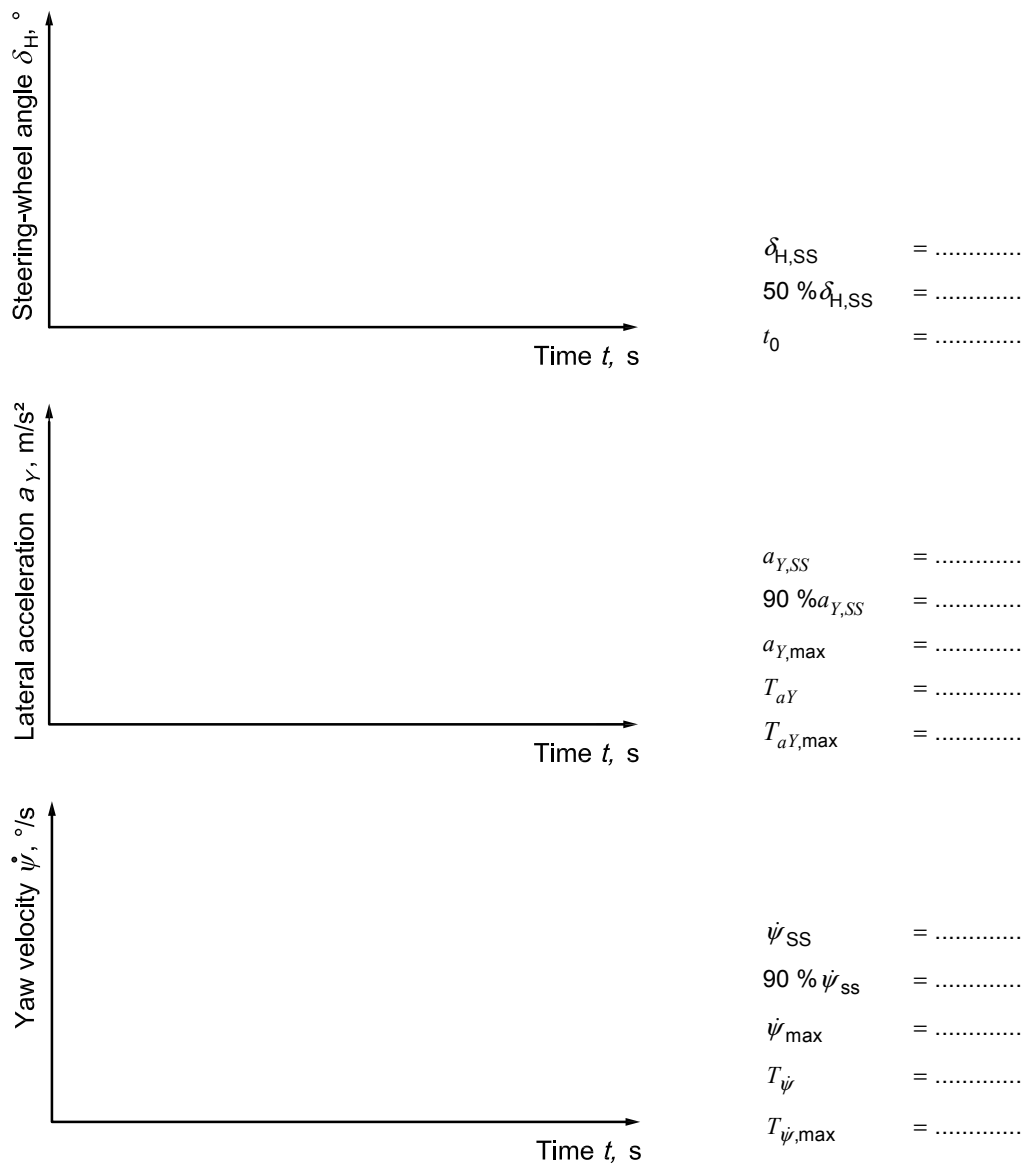
**Test report — Presentation of results**

**B.1 Step input**

Test number: .....

$v_X = 100$  km/h ..... km/h

$a_Y = 4$  m/s<sup>2</sup> ..... m/s<sup>2</sup>



**Figure B.1 — Step input — Time histories**

Table B.1 — Step input — Response data summary

| Parameter                               | Symbol  | Unit            | Left turn | Right turn | Average |
|---|---|-----------------|-----------|------------|---------|
| Steady-state yaw velocity response gain | $\left(\frac{\dot{\psi}}{\delta_H}\right)_{ss}$ | s <sup>-1</sup> |           |            |         |
| Lateral acceleration response time      | $T_{aY}$  | s               |           |            |         |
| Yaw velocity response time              | $T_{\dot{\psi}}$                                | s               |           |            |         |
| Lateral acceleration peak response time | $T_{aY,max}$                                    | s               |           |            |         |
| Yaw velocity peak response time         | $T_{\dot{\psi},max}$                            | s               |           |            |         |
| Overshoot value of lateral acceleration | $U_{aY}$  | —               |           |            |         |
| Overshoot value of yaw velocity         | $U_{\dot{\psi}}$                                | —               |           |            |         |

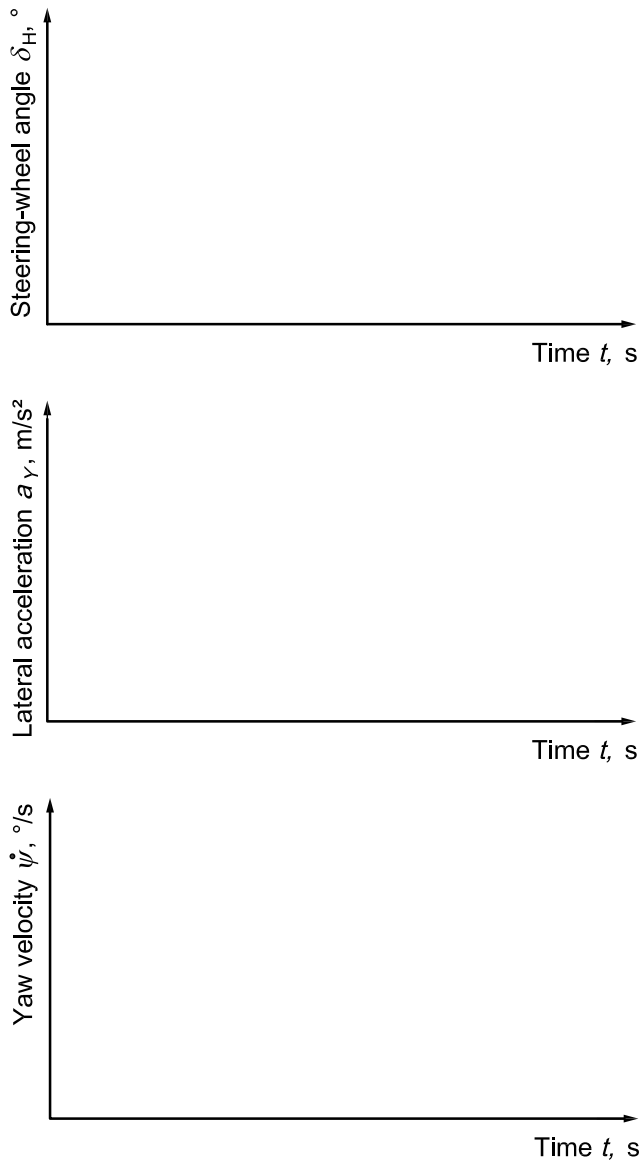
**B.2 Sinusoidal input**

Test number:.....

$v_X = 100$  km/h ..... km/h

$a_Y = 4$  m/s<sup>2</sup> ..... m/s<sup>2</sup>

$f = 0,5$  Hz ..... Hz



**Figure B.2 — Sinusoidal input (one period) — Time histories**



Table B.2 — Sinusoidal input (one period) — Response data summary

| Parameter  | Symbol                        | Unit                    | Left turn  |                    | Right turn |                    |
|--|-------------------------------|-------------------------|------------|--------------------|------------|--------------------|
|  |                               |                         | Mean value | Standard deviation | Mean value | Standard deviation |
| Time lag between steering-wheel angle and lateral acceleration | $T(\delta_H - a_Y)$           |                         |            |                    |            |                    |
| Peak 1   | $T(\delta_H - a_Y)_1$         | ms                      |            |                    |            |                    |
| Peak 2   | $T(\delta_H - a_Y)_2$         | ms                      |            |                    |            |                    |
| Time lag between steering-wheel angle and yaw velocity         | $T(\delta_H - \dot{\psi})$    |                         |            |                    |            |                    |
| Peak 1   | $T(\delta_H - \dot{\psi})_1$  | ms                      |            |                    |            |                    |
| Peak 2   | $T(\delta_H - \dot{\psi})_2$  | ms                      |            |                    |            |                    |
| Lateral acceleration gain                                      | $\frac{a_Y}{\delta_H}$        | $(\text{m/s}^2)/^\circ$ |            |                    |            |                    |
| Yaw velocity gain  | $\frac{\dot{\psi}}{\delta_H}$ | $\text{s}^{-1}$         |            |                    |            |                    |

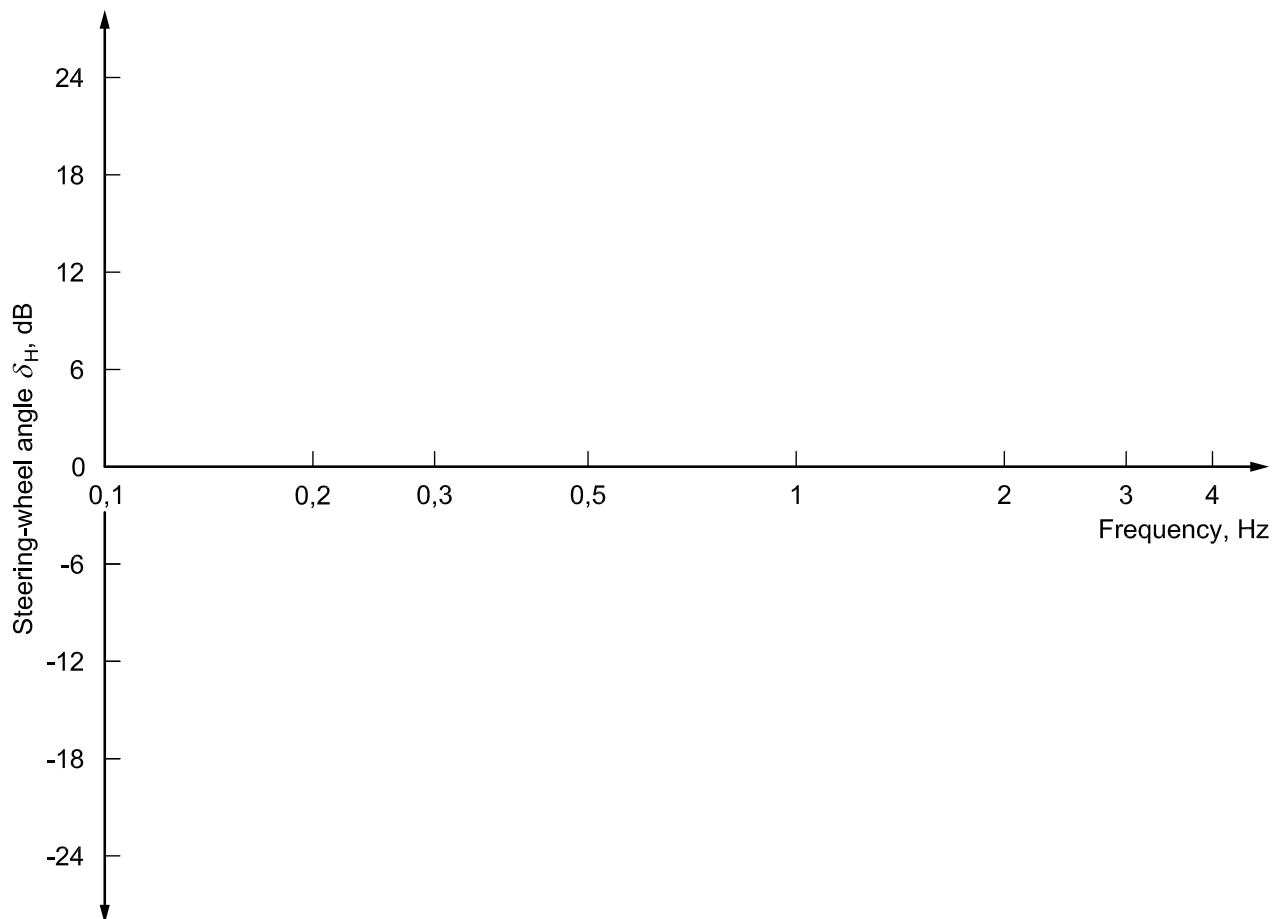
**B.3 Random/pulse<sup>2)</sup> input**

Test number:.....

$v_X = 100$  km/h ..... km/h

$a_Y = 4$  m/s<sup>2</sup> ..... m/s<sup>2</sup>

$f = 0,5$  Hz ..... Hz



Optional is a linear scale for the frequency ( $X$ -axis).

**Figure B.3 — Random/pulse input — Harmonic content of steering-wheel angle**

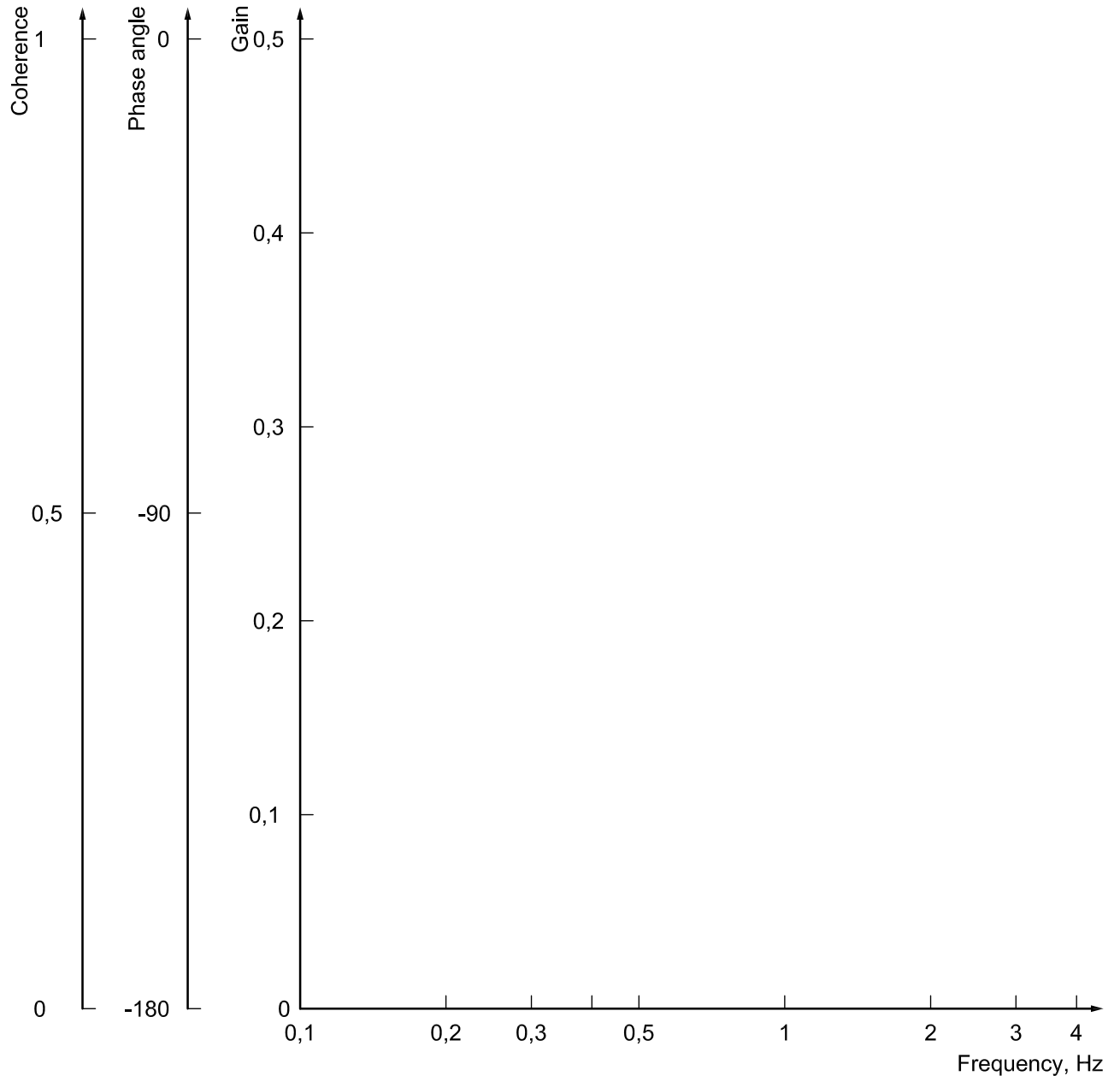
2) Delete as applicable.

**B.4 Random/pulse/continuous<sup>3)</sup> sinusoidal input**

Test number: .....

$v_X = 100 \text{ km/h}$  ..... km/h

$a_Y = 4 \text{ m/s}^2$  .....  $\text{m/s}^2$



Optional is a linear scale for the frequency (*X*-axis).

**Figure B.4 — Random/pulse/continuous sinusoidal input — Transient response to steering-wheel angle**

3) Delete as applicable.

## Bibliography

- [1] ISO 4138, *Passenger cars — Steady-state circular driving behaviour — Open-loop test methods*
- [2] ISO 3833, *Road vehicles — Types — Terms and definitions*
- [3] ECE Regulation No. 30, *Uniform provisions concerning the approval of pneumatic tyres for motor vehicles and their trailers*



